UNIVERSITÄT ZU LÜBECK
INSTITUTE FOR SOFTWARE ENGINEERING
AND PROGRAMMING LANGUAGES

Intermediate Representaions

Concepts of Programming Languages (CoPL)

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November 16, 2015

Overview

We need Compilers!

Classical Compiler Process

Machine Models
- Stack Machines
- Register Machines

Implementations
- LLVM
- CIL

Conclusion

Developing Software

We need compilers!

We need Compilers!

Classical Compiler Process

Machine Models

Stack Machines

Register Machines

Three-Address Code

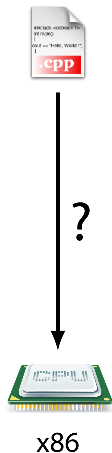
Static-Single-Assignment

Implementations

LLVM

CIL

Conclusion



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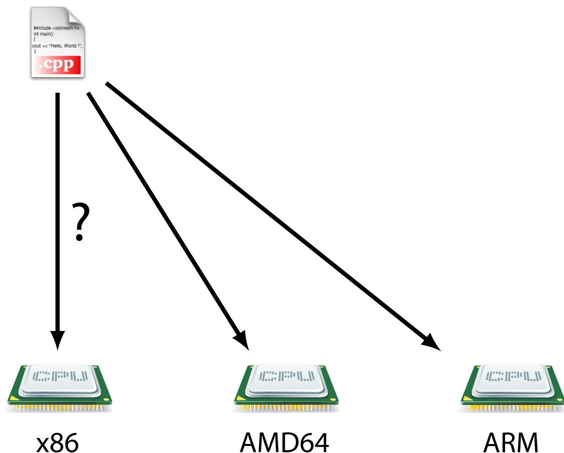

Developing Software

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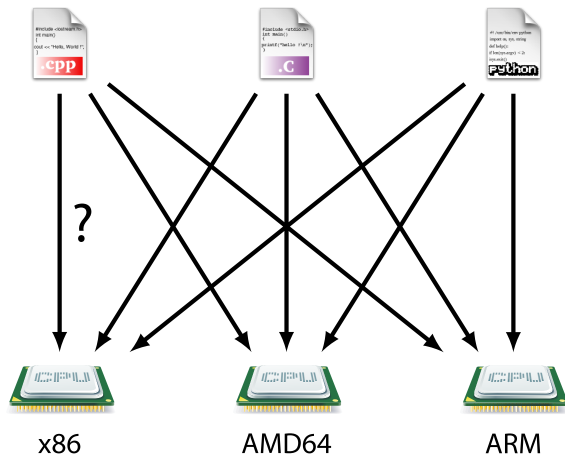

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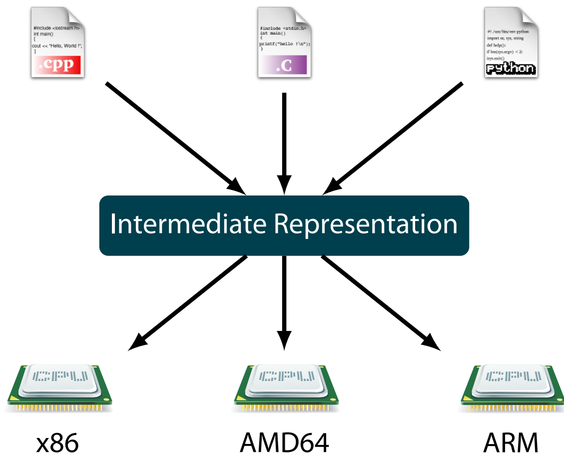
Intermediate Representation

The solution!



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Intermediate Representation

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Definition

An *intermediate representation* (IR) is data structure as representation of a program between a high-level programming language and machine code.

An *intermediate language* (IL) is a low-level assembly language as IR for a virtual machine.

Classical Compiler Process

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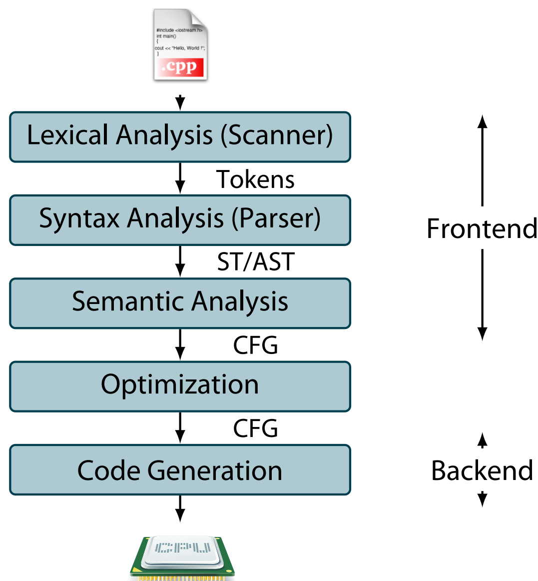


Frontend

Backend

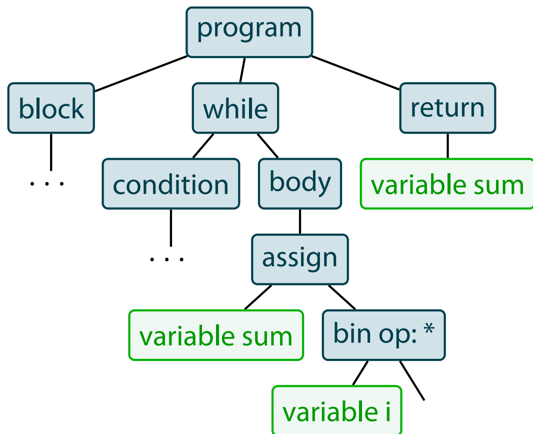
Abstract Sytax Tree

An *abstract syntax tree (AST)* . . .

. . . describes the syntactical structure of a program

. . . depends on the programming language

. . . is generated during by the parser



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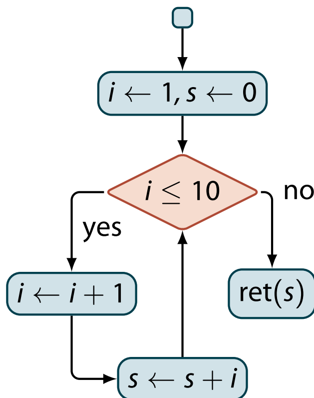
Control-Flow-Graph

```
int s = 1;
for(int i=1; i<=10; i++)
  s += i;
return (s);
```



Stack Machines

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Definition

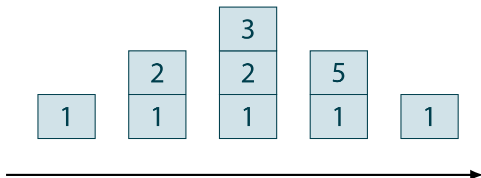
A general *Stack Machine* has

- a stack as storage
- a set of instructions / operations $\mathtt{op} = F(a_1, a_2, \ldots, a_n)$ including (`push` and `pop`)

Executing an operation takes the arguments from top of the stack, computes the result in the accumulator, and pushes the result back the stack.

Example

```
push 1
push 2
push 3
add
pop
```



Stack-machines

Code Generation

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We can generate the control by traversing the syntax tree.
Assume we have to compute the expression $\sqrt{x^2 + y^2}$.

Stack-machines

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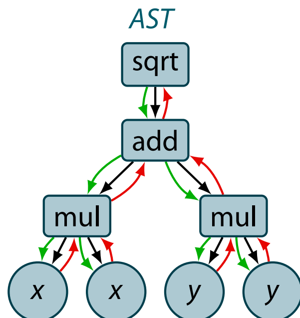


```
push x
push x
mul
push y
push y
mul
add
sqrt
```

Stack Machines

Summary

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- Programs for stack machines are short
  Only the opcodes (or constants) in the byte code.
- In practical use stack machines can be extended
  1. An external memory to store and load values (computations are still limited to the stack)
  2. Top-Level registers
  3. Metainformations (see CIL later)
- Problem: Most processor-architectures use registers.
  $\Rightarrow$ Hybrid Models, Special informations in the intermediate representation.

Register Machines

Definition

A *register machine* . . .

- consists of an infinite number of memory cells named *registers*
- each register is accessible
- has a limited set of instruction / operations:
  1. Arithmetical Operations: Computes a function F using selected registers $\langle o_1, \rangle \ldots, \langle o_n \rangle$ as operands and stores the result in a target register $\langle r \rangle$
  2. Jumps/Branches

Three-Address Code (3AC/TAC)

We need Compilers!

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Conclusion

- Each TAC is a sequence of instructions $I_1, I_2, \ldots, I_n$ for a register machine.
- Instructions can be
  1. Assignments `r1 := r0`
  2. Unconditional Jumps (Instructions can be labeled)

     ```
     L0: goto L1
     ...
     L1: r0 := 1
     ```

  3. Conditional Branches

     ```
     if a<b then goto L1
     ```

  4. Arithmetical operations `r3 := add(r1,r2)`
- Each instruction contains at most *3* registers

Three-Address Code (3AC/TAC)

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     ```

  4. Arithmetical operations `r3 := add(r1,r2)`
- Each instruction contains at most *3* registers

Example ($\sqrt{x^2 + y^2}$)

```
t1 :=  x * x
t2 :=  y * y
t3 := t1 + t2
result := sqrt(t3)
```

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Three-Address Code (3AC/TAC)

How to design the Byte-Code

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For practical use we should store TAC in byte code format.

- Each operation has an *opcode* for the virtual machine
- Each instruction can be represented by tuples

Quadruples

	opcode	op1	op2
t1	MUL	x	x
t2	MUL	y	y
t1	ADD	t1	t2
res	SQRT	t1	-

Triples

opcode	op1	op2
MUL	x	x
MUL	y	y
ADD	(1)	(2)
SQRT	(3)	-

Note

Registers can be assigned implicitly (Triples). But then each register has to be assigned only once.

Static-Single-Assignment

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Definition (Static-Single Assignment)

A Three-Adress Code is in *Static-Single Assignment*-from if each register gets assigned once in the code.

Example ($\sqrt{x^2 + y^2}$)

Not in SSA

```
L1: x := x * x
L2: y := y * y
L3: x := x + y
L4: z := sqrt(x)
```

SSA

```
L1: x0 := x * x
L2: y0 := y * y
L3: x1 := x0 + y0
L4: z  := sqrt(x1)
```

Static-Single-Assigment

How to get SSA-form?

A simple Algorithm

- For each used register: $\langle R \rangle$
  1. Check if $\langle R \rangle$ gets assigned more than once
  2. For each assignment/definition of $\langle R \rangle$:
     - Rename on the left side to $\langle R.i \rangle$ if this assignment is the i-th assignment to $\langle R \rangle$
  3. For each use of $\langle R \rangle$:
     - Replace $\langle R \rangle$ with $\langle R.j \rangle$ where $\langle R.j \rangle$ was the previous replacement for $\langle R \rangle$.

Is this algorithm correct?

Static-Single-Assigment

How to get SSA-form?

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A simple Algorithm

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  3. For each use of $\langle R \rangle$:
     - Replace $\langle R \rangle$ with $\langle R.j \rangle$ where $\langle R.j \rangle$ was the previous replacement for $\langle R \rangle$.

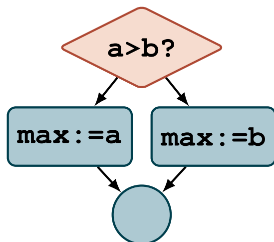
Is this algorithm correct?

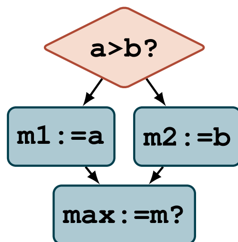
No!

Static-Single-Assignment

What if we have branches?

```
  if a>b then goto L_A
  max := b;
  goto L_END
L_A:
  max := a;
  goto L_END
L_END:
```





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Static-Single-Assignment

The Φ-function

We need Compilers!

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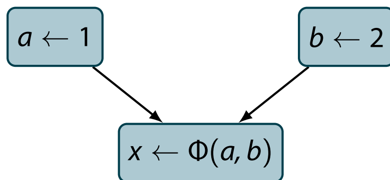
Conclusion

The Φ-*function* computes the value depending on the incoming branch.



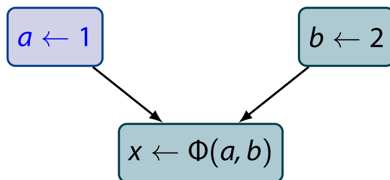
Note

There is no real operation like Φ in real machines. After optimization Φ-statements have to be removed.

Static-Single-Assignment

The Φ-function

The Φ-*function* computes the value depending on the incoming branch.



x has value 1

Note

There is no real operation like Φ in real machines. After optimization Φ-statements have to be removed.

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Static-Single-Assignment

The Φ-function

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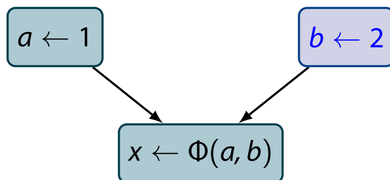

x has value 2

Note

There is no real operation like Φ in real machines. After optimization Φ-statements have to be removed.

Getting Code in SSA-form.

We need Compilers!

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```
L1:
if r_a < r_b then goto L3:
L2:
t_1 := r_a
goto L4

L3:
t_2 := r_b
goto L4

L4: max := phi t_1 [from L2], t_2 [from L3]
```

Converting to SSA-Form

We need Compilers!

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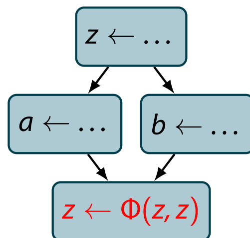
1. Place Φ-function terms
2. Rename registers to achieve SSA-form



Using the Φ-function after each branch for previous registers is an unpractical solution.

Dominance Frontiers

We need Compilers!

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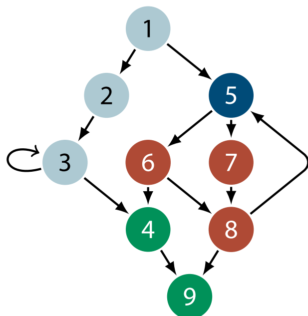
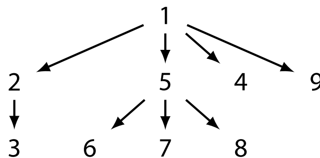
Definition

We say *x dominates y* (x dom y) if on all paths to Y in the CFG the program has to run over X.

Definition

y is in the *dominance frontier* of x (DF(x)) iff not x dom y and y has a direct predecessor on all paths to y



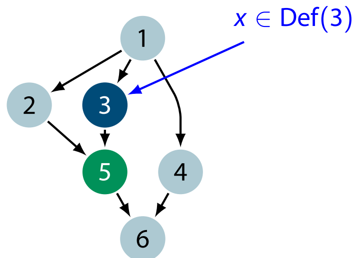


$\text{DOM}(5) = \{5, 6, 7, 8\}$

$\text{DF}(5) = \{4, 9\}$

Dominance Frontiers

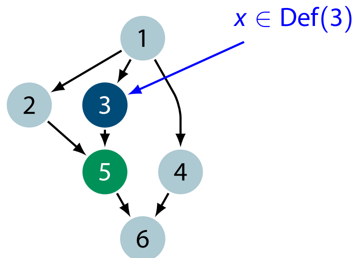
Assume that node 3 defines variable x, $\text{DF}(3) = \{5\}$



Is 5 the only node we need to insert a Φ-function for x?

Dominance Frontiers

Assume that node 3 defines variable x, $\mathrm{DF}(3) = \{5\}$



Is 5 the only node we need to insert a Φ-function for x?

No, at node 6. Why?

Architecture of the LLVM-compiler process

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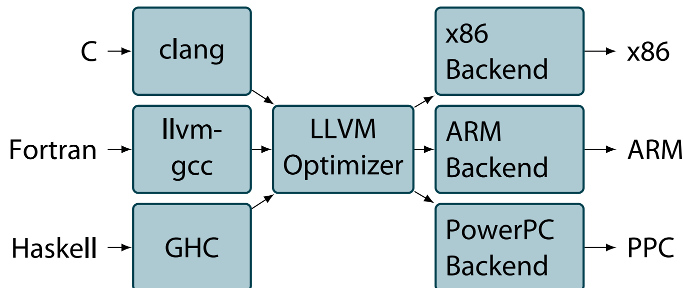
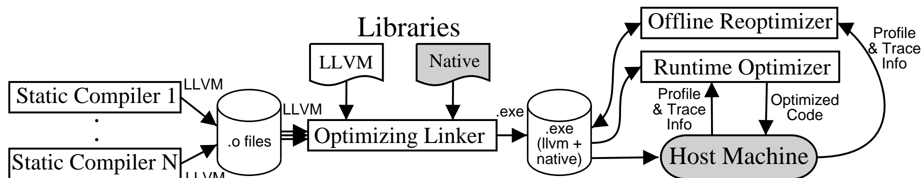


LLVM uses a special intermediate representation (LLVM-IR) for a virtual register machine.

LLVM Compilation Strategy



C. Lattner, The LLVM Instruction Set and Compilation Strategy, 2002

LLVM-IR

```
@.str = private unnamed_addr constant [11 x i8] c"
    ␣%d␣<=␣%d␣\00", align 1

; Function Attrs: nounwind uwtable
define void @minmax(i32 %a, i32 %b) #0 {
  %1 = icmp sgt i32 %a, %b
  br i1 %1, label %2, label %3

  ; <label>:2                         ; preds = %0
  br label %4

  ; <label>:3                         ; preds = %0
  br label %4

  ; <label>:4                         ; preds = %3, %2
  %max.0 = phi i32 [ %a, %2 ], [ %b, %3 ]
  %min.0 = phi i32 [ %b, %2 ], [ %a, %3 ]
  %5 = call i32 (i8*, ...) @printf(i8*
    getelementptr inbounds ([11 x i8], [11 x i8]*
    @.str, i32 0, i32 0), i32 %min.0, i32 %max.0)
  ret void
}
```

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LLVM-IR

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- LLVM is register-based. Registers are written as `%<registername>` (e.g. `%R1 = ...`)
  `@` is used for global variables (e.g. function names)
- LLVM use types `i1, i8, i32` for boolean, Byte and 32-Bit Integer values
- Reduced instruction-set
  - Memory Access `%ptr = alloca i32`
  - Comparing `%res = icmp <opt> <type> %a, %b`
- Conditional Branches
  `br i1 %cond, label %IfLabel, label %ElseLabel`
- Function calls `%res = call`
- `phi`-Instruction for assignments depending on the control flow
- Functions:
  `define <type> @FctName(<type> %arg1,...){...}`
- Metadata

LLVM-IR

```
@.str = private unnamed_addr constant [11 x i8]
  c"␣%d␣<=␣%d␣\00", align 1

; Function Attrs: nounwind uwtable
define void @minmax(i32 %a, i32 %b) #0 {
%1 = icmp sgt i32 %a, %b
br i1 %1, label %2, label %3

; <label>:2                          ; preds = %0
br label %4

; <label>:3                          ; preds = %0
br label %4

; <label>:4                          ; preds = %3, %2
%max.0 = phi i32 [ %a, %2 ], [ %b, %3 ]
%min.0 = phi i32 [ %b, %2 ], [ %a, %3 ]
%5 = call i32 (i8*, ...) @printf(i8*
  getelementptr inbounds ([11 x i8], [11 x i8]*
  @.str, i32 0, i32 0), i32 %min.0, i32 %max.0)
ret void
}
```

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LLVM-IR

Another example

```
define i32 @main() #0 {
  %c = alloca [10 x i32], align 16
  br label %1
1:
  %sum.0 = phi i32 [ 0, %0 ], [ %4, %7 ]
  %i.0   = phi i32 [ 1, %0 ], [ %8, %7 ]
  %2 = icmp sle i32 %i.0, 10
  br i1 %2, label %3, label %9
3:                                          ; preds = %1
  %4 = add nsw i32 %sum.0, %i.0
  %5 = sext i32 %i.0 to i64
  %6 = getelementptr inbounds [10 x i32], [10 x
    i32]* %c, i32 0, i64 %5
  store i32 %4, i32* %6, align 4
  br label %7
7:                                          ; preds = %3
  %8 = add nsw i32 %i.0, 1
  br label %1
9:                                          ; preds = %1
  ret i32 0
}
```

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Common Intermediate Language

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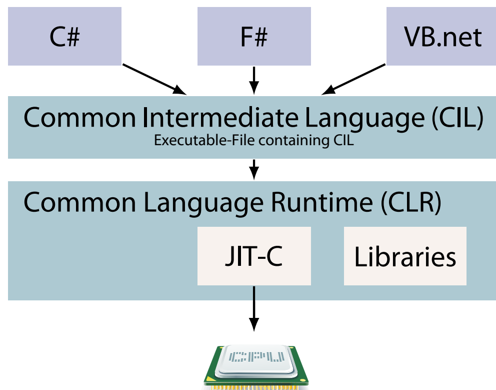

Common Language Infrastructure (CLI)

The CLR is the CLI-Implementation of Microsoft and part of the .net-Framework. The CLI also speciefies a Type System (CTS) and a basic set of class libraries.

CIL

- Stack based virtual machine.
- Each method has a header
- Typed instruction-set (e. g. `ldc.i4.0` load constant 0 as 4-Byte int)
- Access to local variables `ldloc.<index>`, `stloc.<index>`
- Object oriented
  - Load field values `ldfld string Program/Person::prename`
  - Create new objects `newobj instance void class <CLASS>'.ctor'(...)`

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An Example

```
.method public static hidebysig
 default int32 sum (int32 a, int32 b)  cil
managed {
 .maxstack 2
 .locals init (int32 V_0, int32  V_1)
 IL_0000:  ldc.i4.0    //
 ...
 }
```


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Conclusion

CIL

An Example

```
IL_0000:  ldc.i4.0     //
IL_0001:  stloc.0      // sum = 0
IL_0002:  ldarg.0      // load a on the stack
IL_0003:  stloc.1      // store a in first var
(i=a)
IL_0004:  br IL_0011   // --+
IL_0009:  ldloc.0      //   |    <--+
IL_000a:  ldloc.1      //   |       |
IL_000b:  add          //   |
IL_000c:  stloc.0      //   |
IL_000d:  ldloc.1      //   |
IL_000e:  ldc.i4.1     //   |
IL_000f:  add          //   |       .
IL_0010:  stloc.1      //   |       .
IL_0011:  ldloc.1      // <-+       .
IL_0012:  ldarg.1      // load b    |
IL_0013:  ble IL_0009 // i<=b     -+
IL_0018:  ldloc.0
IL_0019:  ret
```

Conclusion

We need Compilers!
Classical Compiler Process
Machine Models
Stack Machines
Register Machines
Three-Address Code
Static-Single-Assignment
Implementations
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Intermediate Representations . . .

- allow a clean and general compiler-architecture/infrastructure
- allow mixing different programming languages
- programmer may loose control on the real control-flow
- program-flow can be optimized
- adaption to different hardware configurations (including GPU-support).
- improve the development of new programming languages
- can realize translations between different languages

We need Compilers!

Classical Compiler Process

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Any Questions?